Probabilistic Nano-Mechanical Finite Weakest-Link Model for Quasibrittle Structure Strength, Crack Growth, Lifetime and Fatigue

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Abstract: The size effect on structural strength and its statistical distribution is a complex problem for quasibrittle materials because their failure behavior transits from quasi-plastic at small sizes to brittle at large sizes. These are heterogeneous materials with brittle constituents in which the inhomogeneinty size is not negligible compared to the structure size. They are exemplified by concrete, as the archetypical example, fiber composites, coarse-grained ceramics, rocks, sea ice, wood, bone, foam, masonry etc., and all brittle materials at the micro- or nano-scale. The lecture begins by reviewing the statistical and energetic size effect on the mean strength of quasibrittle structures. Kramer's rule of transition rate theory for the frequency or probability of nano-crack jumps, and some new simple rules for the multiscale transition to material scale, are used to show that the type of probability distribution of structural strength depends on the structure size and geometry. On the scale of the representative volume element of material, the probability distribution of strength is found to be Gaussian, with a remote Weibullian tail. The structure size effect is based on the weakest-link statistics for a chain whose length is not infinite but finite. For increasing structure size, the Weibullian portion gradually spreads into the Gaussian core and, for very large sizes, the distribution becomes purely Weibullian. Based on an atomistic derivation of the power law for creep crack growth, it is further shown that a similar change of distribution occurs for structure lifetime. The theory is further extended to the size dependence of Paris law and Basquin law for fatigue fracture and statistics of fatigue lifetime. Based only on a few common hypotheses, the theory describes well the existing experimental results on the monotonic strength, static and fatigue crack growth rate, and static and fatigue lifetimes, and ceramic micro-devices, must depend on their size and shape. Another is that the static and comp Abstract: The size effect on structural strength and its statistical distribution is a complex problem for quasibrittle for computer analysis of quasibrittle structures are outlined.

Bio-Sketch: Born and educated in Prague (Ph.D. 1963), Bažant joined Northwestern in 1969, where he has been W.P. Murphy **Bio-Sketch:** Born and educated in Prague (Ph.D. 1963), Bažant joined Northwestern in 1969, where he has been W.P. Murphy Professor since 1990 and simultaneously McCormick Institute Professor since 2002, and Director of Center for Geomaterials (1981-87). He was inducted to National Academy of Sciences, National Academy of Engrg. and Am. Acad. of Arts & Aci., as well as Italian Nat. Acad. (dei Lincei), Austrian Acad. of Sciences, Spanish Royal Acad. of Engrg., Czech Acad. of Engrg., Istituto Lombardo and Eur. Acad. of Sci. & Arts. An Hon. Member of ASME, ASCE and ACI, and an Illinois Registered Structural Engineer, he received seven honorary doctorates (Prague, Karlsruhe, Colorado-Boulder, Milan, Lyon, Vienna, Ohio State), ASCE von Karman, Newmark, Biot and Croes Medals and Lifetime Achievement Award, SES Prager Medal, ASME Timoshenko, Warner and Nadai Medals, RILEM L'Hermite Medal, Torroja Medal, etc. He authored six books: Scaling of Structural Strength, Inelastic Analysis, Fracture and Size Effect, Stability of Structures, Concrete at High Temperatures, and Concrete Creep. H-index: 89, citations: 35,000 (on Google, minus ~10% self-citations), i10 index:434. He is one of the original top 100 ISI Highly Cited Scientists in engineering (www.ISIhighlycited.com).

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